

# Geodesy 1B

## Lecture 2

### Precise Leveling

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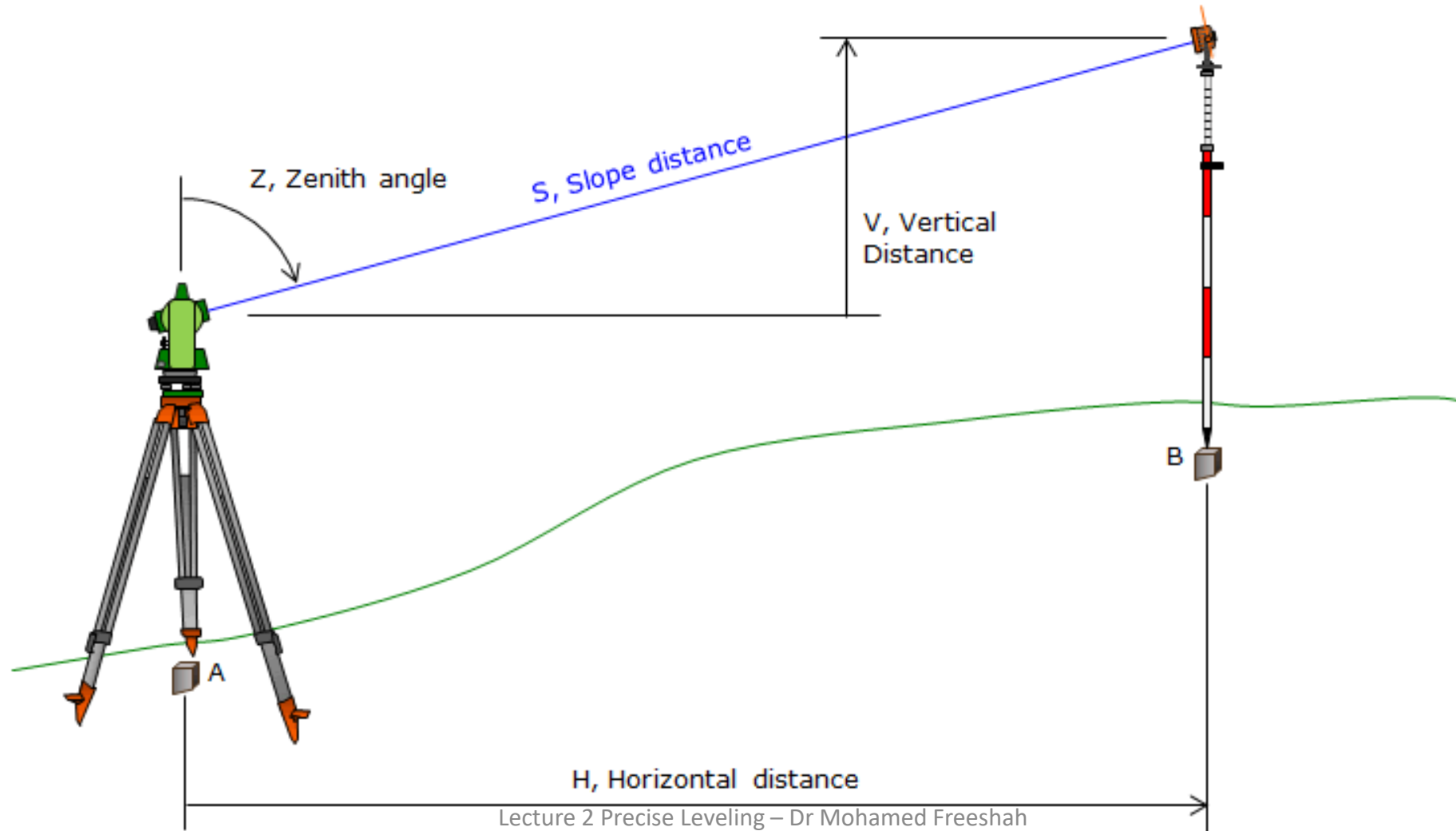
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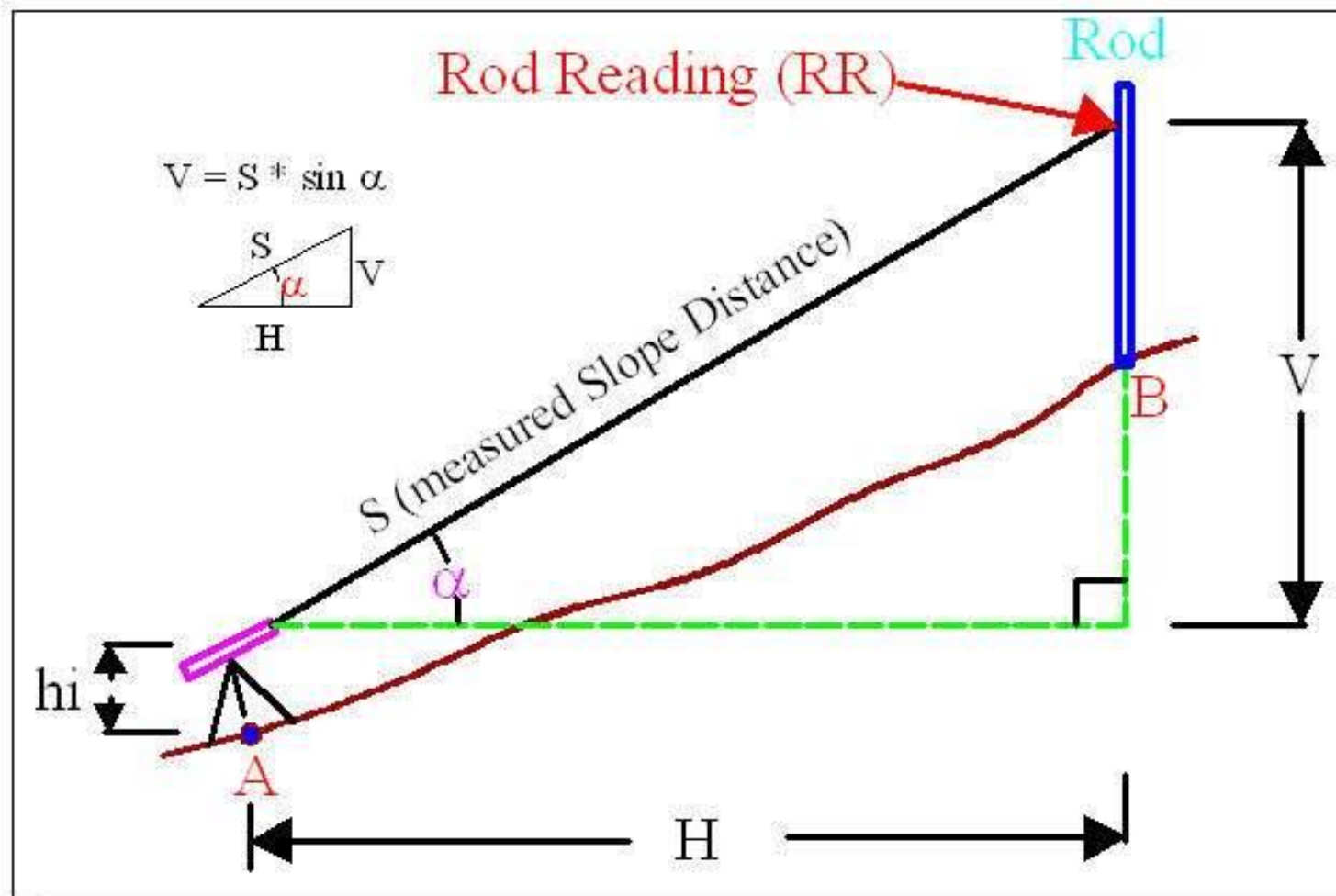
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- Review and ideas of trigonometric leveling
- Important definitions
- Precise leveling
- Correction of P.L
- Applications of P.L
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# Trigonometric Levelling in small areas, Total Station mechanism



# Trigonometric Levelling in small areas, Total Station mechanism



# Important Definitions

## 1- LEVELLING

- *Levelling* is an operation in surveying performed to determine the difference in levels of two points. By this operation the height of a point from a *datum*, known as *elevation*.

## 2- LEVEL SURFACE

- A *level surface* is the **equipotential** surface of the earth's gravity field. It is a curved surface and every element of which is normal to the plumb line.

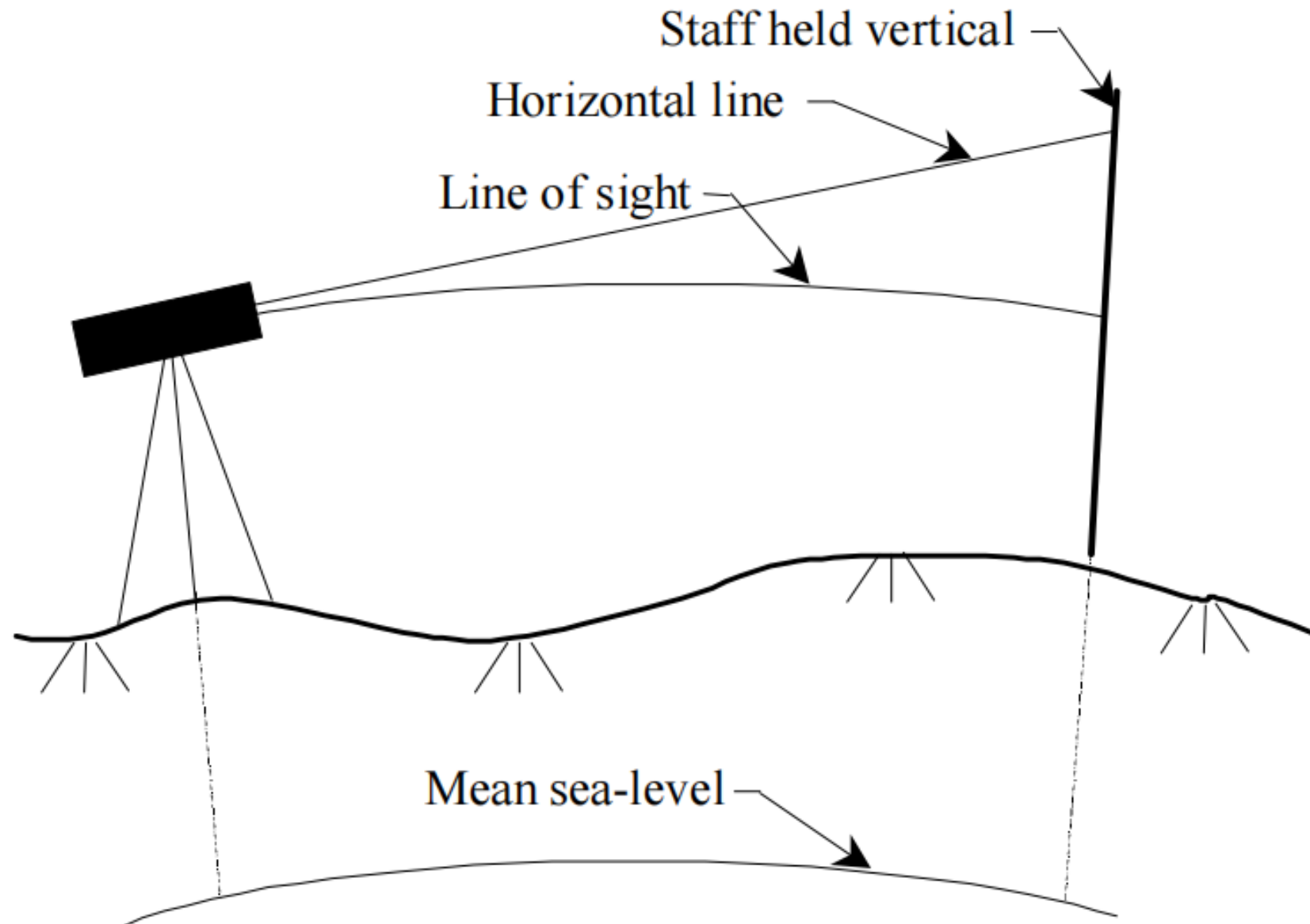
# Important Definitions

## 3- DATUM

- A *datum* is a reference surface of constant potential, called as a level surface of the earth's gravity field, for measuring the elevations of the points. One of such surfaces is the **MSL** surface and is considered as a standard datum. Also **arbitrary** surface adopted as a datum.

## 4- LEVEL LINE

- A line lying in a level surface is a *level line*. It is thus a curved line.

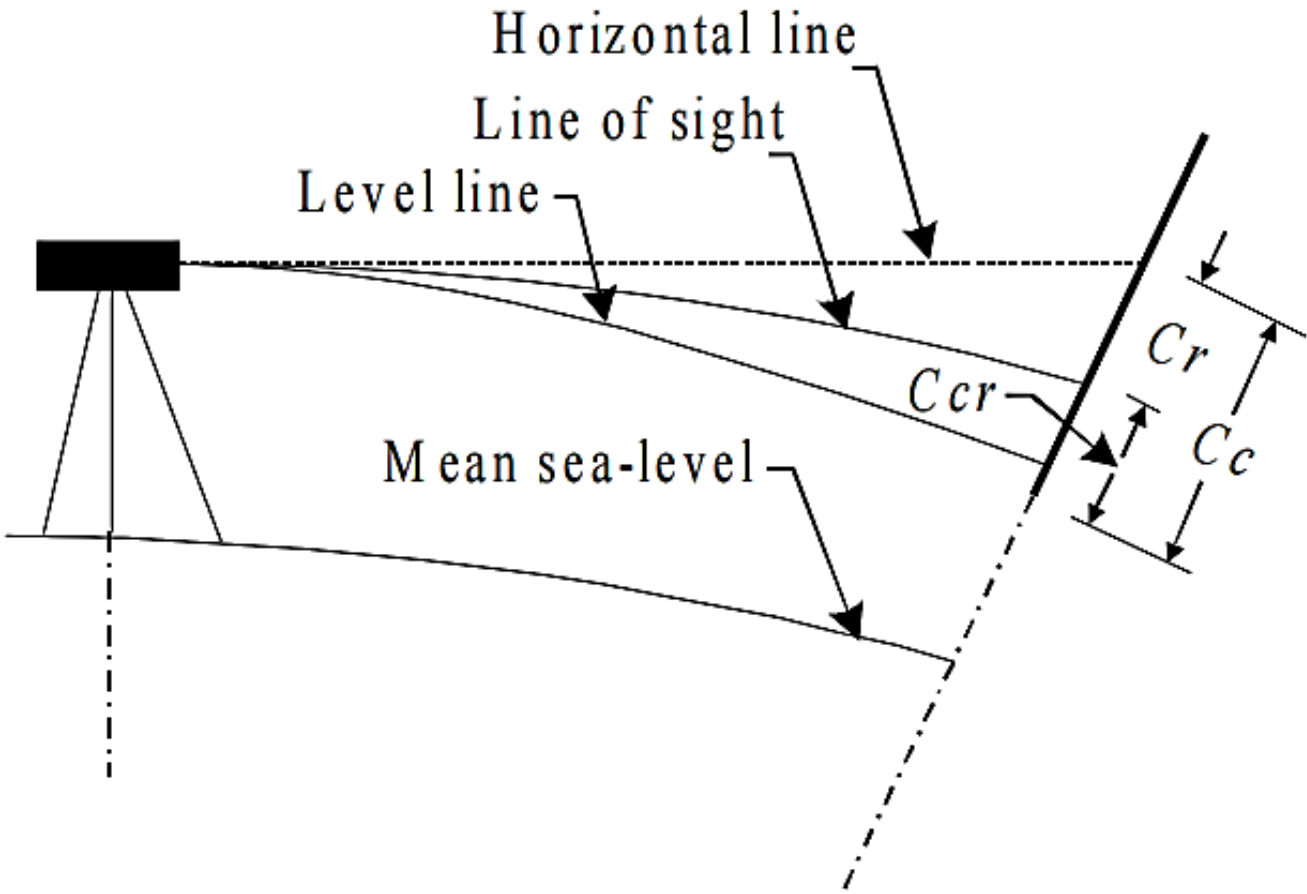


# Precise Leveling

- This is the operation of levelling in which precise instruments are used. It is used for establishing bench marks for future public work.
- In principle, no difference between ordinary and precise leveling.
- In the former, distances between check points are short, elevations are satisfactory for routine purposes.
- Efforts to control all the sources of errors (balancing of B.S and F.S, equal length of sights...etc.)
- Read temperatures to correct graduations along the length of staff, also, coefficient of refraction. Shimmering (near foot of staff)
- Unequal expansion of instrument parts (keep it in shade)



# Precise Leveling Corrections



# Precise Leveling Corrections

- The corrections for the curvature of the level line  $C_c$  and refraction  $C_r$  are shown in
- The combined correction is given by

$$C_{cr} = -\frac{3d^2}{7R} \quad \dots(3.1)$$

where

$C_{cr}$  = the correction for the curvature and refraction,

$d$  = the distance of the staff from the point of tangency, and

$R$  = the mean earth's radius.

For the value of  $R = 6370$  km and  $d$  in kilometre, the value of  $C_{cr}$  in metre is given as

$$C_{cr} = -0.067d^2 \quad \dots(3.2)$$

# Loop Closure

- A *loop closure* or *misclosure* is the amount by which a level circuit fails to close. It is the difference
- of elevation of the measured or computed elevation and known or established elevation of the same
- point. Thus loop closure is given by

$$e = \text{computed value of R.L.} - \text{known value of R.L.}$$

- If the length of the loop or circuit is  $L$  and the distance of a station to which the correction
- $c$  is computed, is  $l$ , then

$$c = -e \frac{l}{L}$$

# Precise level differ from ordinary level

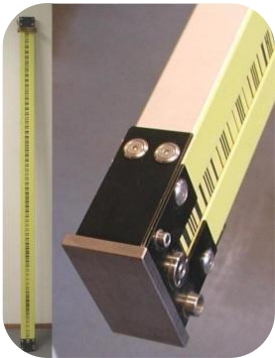
- The leveling base is made broad and part of instrument is reduced in height. (stability)
- The bubble tube curvature is made large to increase sensitivity
- Magnification of telescope (aperture of telescope at least 4 cm)
- A parallel plate micrometer to read staff directly 0.001 m

# Invar precision leveling staff

- Invar (an alloy of iron and nickel with a negligible coefficient of expansion, used in the making of clocks and scientific instruments.)
- It is used for precise leveling work. Generally, 3 m long. To mount staff accurately, detachable stays are provided.
- An invar band (5-10 mm thickness) is fitted to the wooden staff.



**Has a circular bubble, Metal base**  
Prevent corrosion of staff base



**More accurate**  
Sometimes min. division 0.5cm  
(double that of ordinary staff)

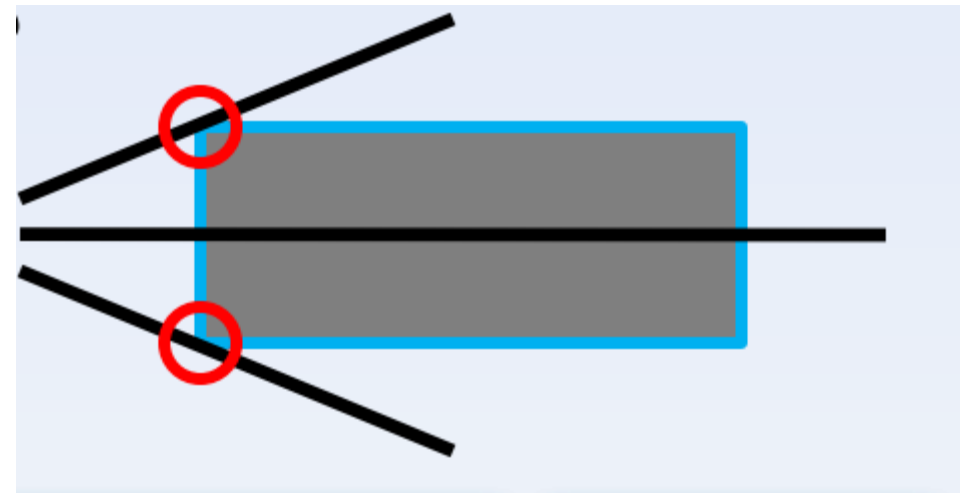
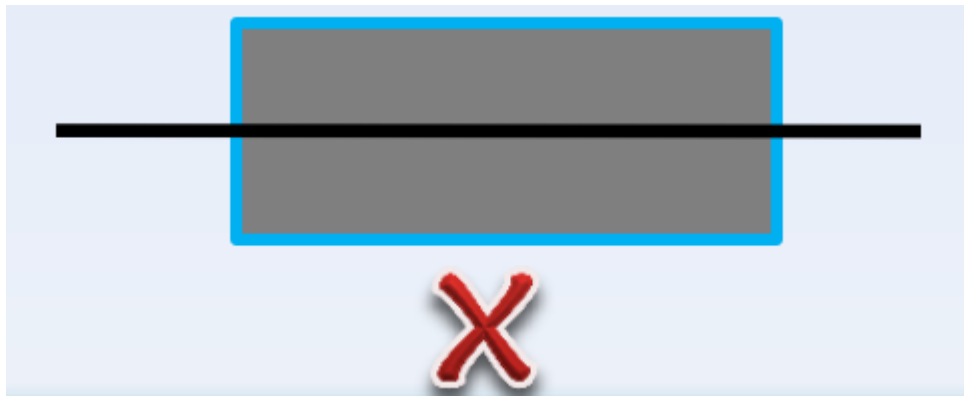


**Micrometer** with certain divisions (50 or usually 100) dividing the min. division of the staff and increasing the final accuracy

# Cross-hair in Precise Levelling

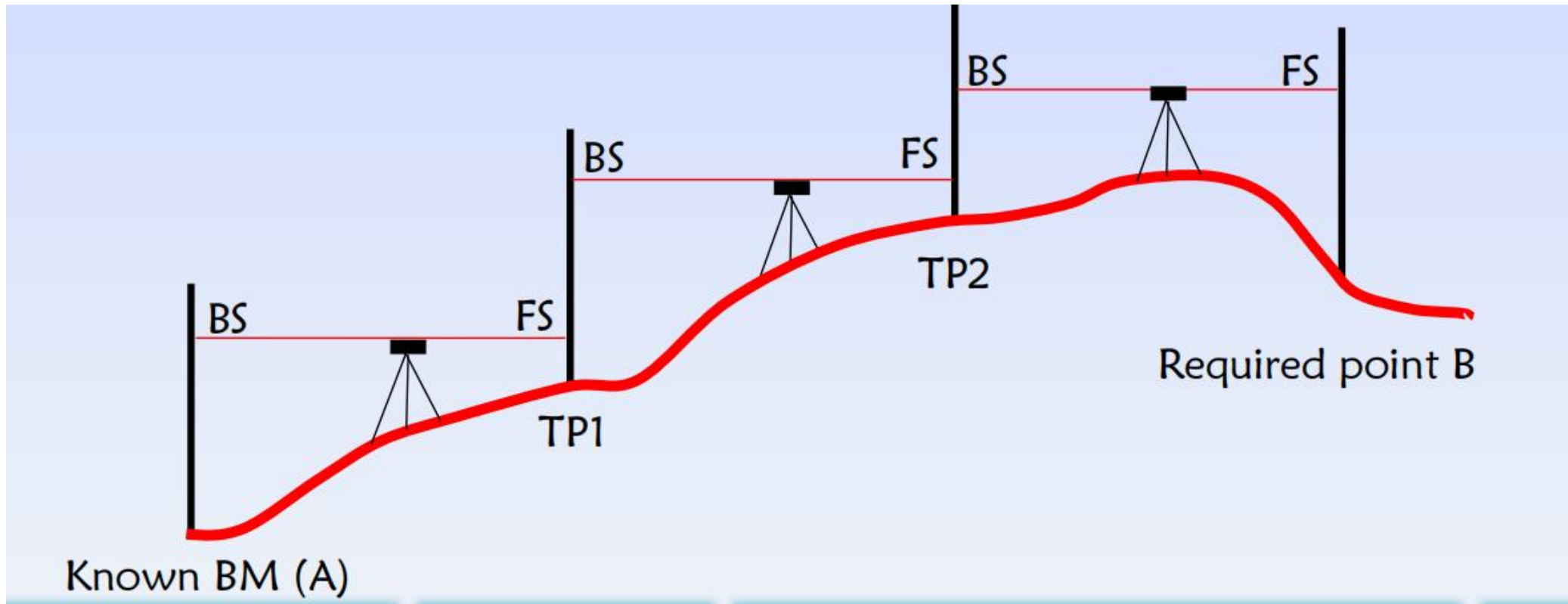
## Wedge cross hair

- Focusing the division on the horizontal cross hair is replaced by focusing on the tangency of the wedge cross hair with the staff division
- Micrometer readings are always added whatever
- focusing on upper or lower division



# Applications of precise leveling

## 1- Benchmark Transfer



# Applications of precise leveling

## 2- Concrete Bridge's Loading Test



Fig 1: - Bridge Load Testing



- Determine the **deformation** of bridges due to ultimate cases of loading
- Check **elasticity** (returning to its original state) or **plasticity** (permanent deformation due to loading) of any bridge after removal of loading.



# Applications of precise leveling

## 2- Concrete Bridge's Loading Test

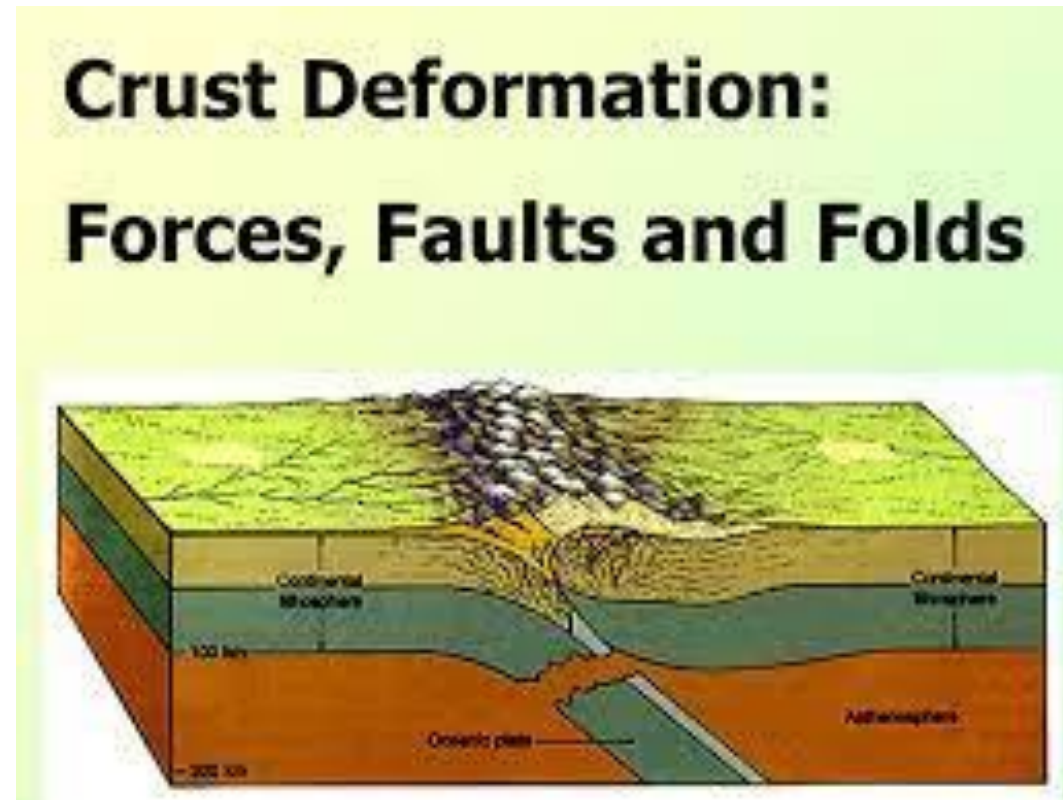
- **How to get Readings?**

- a) Before loading.
- b) Just after loading.
- c) 1 hour after loading.
- d) 2 hours after loading.
- e) Just after loading removal...and so on.



# Applications of precise leveling

## 3- Crust Deformation



Check the **movement** of Earth's surface due to strong force such as **Earthquakes**

# The level page for Precise leveling

Table 6.4 Level book page 3

Station	B.S.	H.I.	F.S.	R.L.	Temperature (°C)	Remarks
	1.530					
1	2.100					B.M.
	2.670					
Mean	2.100	128.425		126.325		
	1.260		1.200			
2	1.900		1.831			T.P.
	2.541		2.463			
Mean	1.900		1.831	126.594		
			1.382			
3		128.494	1.964			
			2.645			
		Mean	1.964	126.530		
$\Sigma \text{ B.S.} - \Sigma \text{ F.S.}$ $= 4.000 - 3.795 = 0.205$				$\text{Last R.L.} - \text{First R.L.}$ $= 126.530 - 126.325 = 0.205$		

# Standards of permissible errors in P.L

- 1<sup>st</sup> order  $\pm 4 (k)^{1/2}$  mm
- 2<sup>nd</sup> order  $\pm 8 (k)^{1/2}$  mm
- 3<sup>rd</sup> order  $\pm 12 (k)^{1/2}$  mm
- K is distance in km

# Calculations of Curvature and Refraction corrections

- Look at white board